

# Design of adapted induction motors for variable-capacity ventilation systems

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## ABSTRACT

The aim of this study is to develop an energy-efficient design approach for adjustable-speed induction motor drives used in variable-capacity ventilation systems. For such applications, the use of induction motors tailored to specific operating conditions is essential. Motor optimization based on an efficiency criterion was performed using the DIMASDrive software (a specialized induction motor design tool), and the complete drive system was modeled in the MATLAB/Simulink environment. Based on the optimization and simulation results, a novel discounted cost criterion evaluated over the full operating speed range of variable-capacity ventilation loads is proposed. The criterion accounts not only for capital costs and energy efficiency, but also for the costs of reactive power and distortion power compensation, thereby reflecting both the energy performance and electromagnetic compatibility of the drive with the supply network—aspects not explicitly addressed in previously reported criteria. Structural and parametric optimization based on the proposed criterion resulted in a 19.5% reduction in the criterion value compared to a design optimized solely by the efficiency criterion, demonstrating the effectiveness and practical relevance of the proposed approach for energy-efficient drive design in ventilation applications.



## 1. Introduction

Variable-capacity ventilation applications are increasingly transitioning from fixed-speed to adjustable-speed drive configurations, which offer substantial reductions in electricity consumption while maintaining the required process conditions.<sup>1–4</sup>

When operated over a variable-speed range, standard general-purpose induction motors (IMs) exhibit suboptimal performance in power density, economic efficiency, and energy characteristics. It is therefore preferable to use specially designed adjustable-speed induction motors (ASIMs) tailored to specific operating conditions.<sup>5–9</sup> Spe-

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cially designed ASIMs are developed by adapting standard general-purpose IMs to the specific operating conditions of the target application in adjustable-speed drives, resulting in superior energy performance compared to non-adapted motors. The adaptation is carried out through structural and parametric optimization with respect to appropriate objective functions, the most widely used of which is efficiency, the primary indicator of energy performance.

The design of an ASIM should begin with the selection of an appropriate baseline IM, typically a standard production motor, which is then adapted for the target application. The fan is represented by the fan load characteristic, that is, by the dependence of the resisting torque on the motor-shaft speed within the specified operating range.

In addition to the conventional efficiency criterion, the design of an ASIM may also be evaluated using an innovative discounted cost criterion (DCC). This criterion considers not only the cost and energy efficiency of the ASIM drive, but also the costs associated with reactive-power compensation and distortion-power compensation. The reactive-power and distortion-power compensation components reflect both the drive's energy performance and its electromagnetic compatibility with the supply network.<sup>10–12</sup>

The DCC provides a comprehensive monetary assessment of drive quality. However, in its current form, this criterion does not account for the cost component associated with distortion-power compensation, leading to an underestimation of the criterion value. A method for calculating this component and incorporating it into the DCC is therefore required.

Because ventilation systems operate under specific load conditions, the selected criteria should be range-based and should account for the operating mode of the fan.<sup>13,14</sup>

Optimization-based design can be carried out using computer-aided tools. In this study, ASIM drive configurations based on different IMs are modeled in MATLAB/Simulink<sup>15–19</sup> and in the DIMAS*Drive* software package. DIMAS*Drive* includes optimization procedures that enable the development of modified ASIMs by varying the structural parameters adopted as design variables within the accepted drive configuration.

The most widely used converters in such systems are two-level transistor frequency converters with autonomous voltage inverters. The ASIM drives considered in this study are analyzed under the proportional control law  $U/f = \text{const}$ .

The advantages of adapted ASIMs over baseline IMs can be achieved by selecting an optimal com-

bination of non-standard voltage and frequency ratings for the designed motor, coordinated with the converter's nominal parameters, while eliminating constraints on starting performance.

## 2. Description of the fan load characteristic

The main characteristic of a ventilation fan is the relationship between the developed total pressure  $H$  and the flow rate  $Q$ . Because these quantities are also specified for different rotational speeds (**Figure 1**), they can be used to construct the fan load characteristic for the ASIM drive. In addition, the fan efficiency values at each rotational speed must be accounted for when determining the shaft power.

The load power is determined by the following expression:

$$P = \frac{Q \cdot H}{\eta_{fan}} \cdot 10^{-3} \quad (1)$$

where  $Q$  is the fan flow rate,  $\text{m}^3/\text{s}$ ;  $H$  is the total pressure, Pa; and  $\eta$  is the fan efficiency.

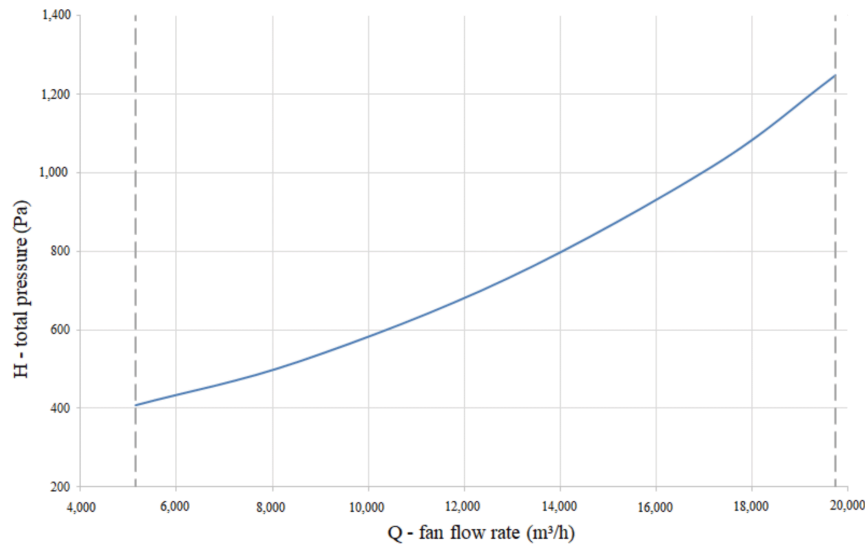
The power is also expressed as  $P = M \cdot \frac{\pi \cdot n}{30}$ . For known rotational speeds, the corresponding load torque values on the motor shaft can be determined. This procedure enables the transition from the  $H$  and  $Q$  relationships under speed control to the construction of the load characteristic  $n(M)$  (**Table 1**).

During speed control, the ventilation system output decreases from the maximum value,  $Q_{max}$ , to the minimum value,  $Q_{min}$ . The specified flow-rate range is  $Q_{max} = 5.48 \text{ m}^3/\text{s}$  and  $Q_{min} = 1.43 \text{ m}^3/\text{s}$ , which corresponds to a fan speed range from  $n_{max} = 2,300 \text{ rpm}$  to  $n_{min} = 600 \text{ rpm}$ . Over the same interval, the total pressure changes from  $H_{max} = 1,247 \text{ Pa}$  to  $H_{min} = 408 \text{ Pa}$ .

When designing an IM for an ASIM drive, the motor and the load must be considered together. Therefore, the comprehensive mathematical model of the drive should also include a mathematical model of the load. The mechanical load acting on the motor shaft is described by the dependence of the resisting torque on angular speed. In the general case, this relationship can be written as follows:

$$M(\omega) = M_0 + k \cdot \omega^i \quad (2)$$

where  $M_0$  is the initial torque,  $\text{N}\cdot\text{m}$ ;  $k$  is the proportionality coefficient;  $\omega$  is the angular speed of the motor shaft,  $\text{s}^{-1}$ ; and  $i$  is the exponent that determines the shape of the load characteristic. Thus, the load torque at a given angular speed depends on three parameters:  $M_0$ ,  $k$ , and  $i$ . These



**Figure 1.** Total pressure–flow rate characteristic of the axial fan

**Table 1.** Transition from the  $H=f(Q)$  characteristic to the  $n=f(M)$  load characteristic

n, rpm	Q, m³/s	Q, m³/h	H, Pa	$\eta_{fan}$	P, kW	M, N·m
600	1.43	5,148	408	0.443	1.3	21
1,000	2.38	8,568	520	0.446	2.8	26.5
1,500	3.58	12,888	730	0.45	5.8	37
2,000	4.77	17,172	1,016	0.454	10.7	51
2,300	5.48	19,728	1,247	0.458	14.9	62

Abbreviations: H: Total pressure; M: Fan load torque; n: Rotational speed; Q: Fan flow rate–fan efficiency; P: Fan power.

parameters are chosen to ensure that the mathematical expression adequately describes the fan’s actual load characteristic.

For centrifugal fan loads, the exponent usually lies in the range  $i = (2 \dots 3)$ . Similar characteristics are also observed for blowers, centrifugal fans, and exhausters. In this study, the fan load torque is assumed to follow a quadratic dependence on rotational speed with a certain initial torque  $M_0$ :

$$M = M_0 + k \cdot n^2 \quad (3)$$

To obtain preliminary values of  $M_0$  and  $k$  for the load characteristic given above, a system of equations is solved:

$$\begin{cases} n_1^2 \cdot x_1 + x_2 = M_1 \\ n_2^2 \cdot x_1 + x_2 = M_2 \end{cases} \quad (4)$$

where  $x_1 = k$  and  $x_2 = M_0$ . Using the extreme points of the speed-control range,  $n_1 = 600 \text{ rpm}$ ,  $M_1 = 21 \text{ N} \cdot \text{m}$ ,  $n_2 = 2,300 \text{ rpm}$ ,  $M_2 = 62 \text{ N} \cdot \text{m}$ , the proportionality coefficient  $k$  and the initial torque  $M_0$  can be determined. In matrix form,

the system can be written as follows:

$$\begin{vmatrix} k \\ M_0 \end{vmatrix} = \begin{vmatrix} n_1^2 & 1 \\ n_2^2 & 1 \end{vmatrix}^{-1} \cdot \begin{vmatrix} M_1 \\ M_2 \end{vmatrix} \quad (5)$$

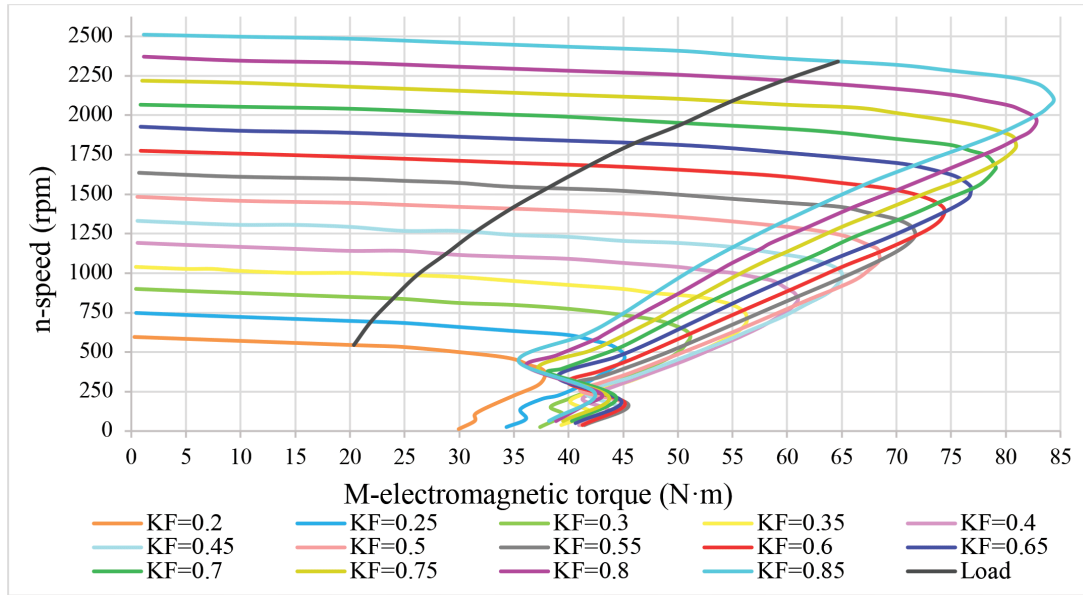
The solution yields the coefficient  $k = 0.0083 \cdot 10^{-3}$ ,  $M_0 = 18.1 \text{ N} \cdot \text{m}$ . The resulting dependence of load torque on fan rotational speed can therefore be written as follows:

$$M = 18.1 + 0.0083 \cdot 10^{-3} \cdot n^2 \quad (6)$$

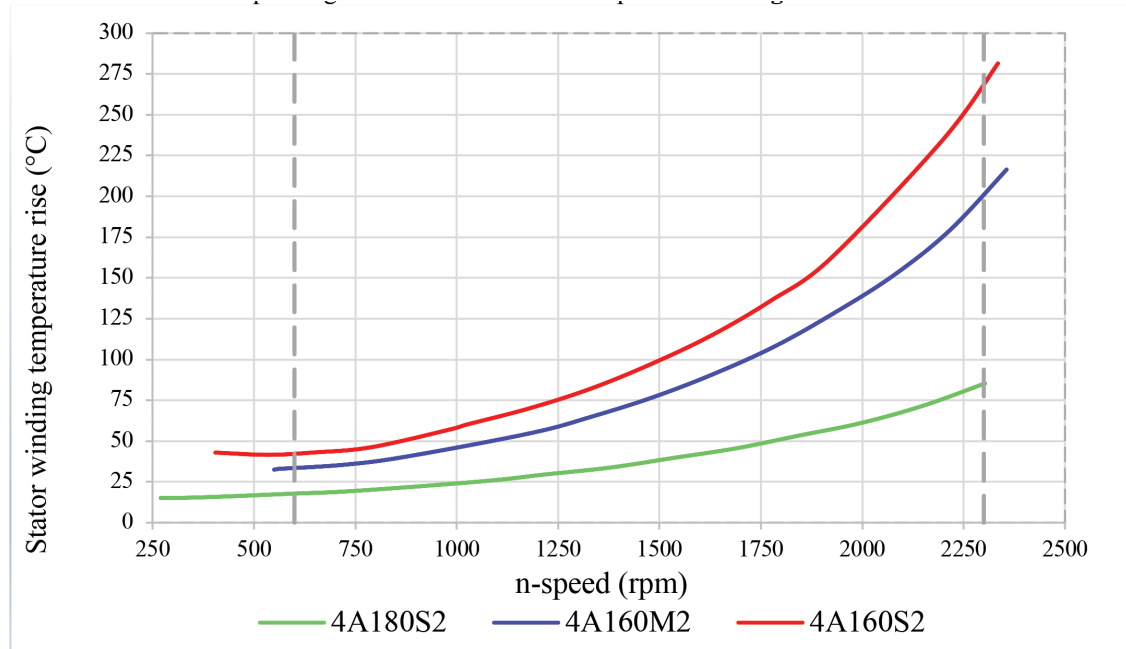
Thus, by adjusting the parameters  $M_0$ ,  $k$ , and  $i$  the fan load characteristic can be approximated with the required accuracy.

### 3. Modeling of the adjustable-speed induction motor drive using DIMASDrive

DIMASDrive enables the simulation of an ASIM drive using mathematical models of its components. The drive systems considered here use identical frequency converters and operate with the same fan load. The configurations differ only in the motor type: the baseline 4A160M2 and two of its modified ASIM versions.



**Figure 2.** Family of mechanical characteristics of the induction motor 4A160M2 and the fan load characteristic



**Figure 3.** Thermal characteristics of the proposed induction motors

For each drive configuration, a family of mechanical characteristics can be constructed together with the superimposed fan load characteristic. The characteristics obtained for the configuration with the baseline 4A160M2 are shown in **Figure 2**.

Based on the thermal-state analysis, in particular the steady-state temperature of the stator phase winding, which is the most thermally stressed motor element, several candidate baseline motors were analyzed in DIMAS*Drive*. The corresponding thermal characteristics are presented in **Figure 3**.

Based on its thermal characteristics, the 4A160M2 motor (18.5 kW) is the most suitable baseline motor for adaptation to the fan operating conditions considered in this study. The 4A180S2 motor (22 kW) operates under a partial load, whereas the 4A160S2 motor (15 kW) and the 4A160M2 motor operate in an overloaded condition at the upper end of the control range, as indicated by the elevated temperature of the stator phase winding (**Figure 3**). Its overload is eliminated through the structural and parametric optimization procedure described in the following section.

#### 4. Optimization-based design in the DIMAS*Drive* environment using the motor efficiency criterion

A systems-level perspective requires the simultaneous treatment of the converter, motor, and load—and, where applicable, the gearbox and supply transformer—as a unified electromechanical system. Therefore, a key feature of ASIM design is the need to use a comprehensive mathematical model of the entire drive rather than a model of the motor alone, as is commonly done for general-purpose IMs. Although modern optimization-based design methods for alternating current electrical machines are well developed, they are mainly intended for conventional machines and are not specifically focused on adapted IMs. Further improvement of mathematical and software tools is therefore required for the effective design of specialized ASIMs. In the optimization-based design of ASIMs, a range-based efficiency criterion can be applied. In this case, the motor energy performance is evaluated using a range-based criterion defined by the range-averaged efficiency over the operating speed range:

$$\eta_{avg} = \frac{1}{n_2 - n_1} \cdot \int_{n_1}^{n_2} \eta(n_i) dn \quad (7)$$

Several modifications of the baseline 4A160M2 motor are proposed. In the first modification, thin cold-rolled isotropic electrical steel grade 2211 is replaced with electrical steel grade 2411. This modification represents a structural optimization of the motor. The specific core losses of steel grade 2211 are  $p = 2.2$  W/kg, whereas for steel grade 2411 they are  $p = 1.3$  W/kg. In the second modification, the design obtained after the first stage is used as the initial configuration, and the stator-winding parameters, the core length, and the geometry of the stator and rotor tooth regions are optimized using the Nelder–Mead simplex method. This stage corresponds to parametric optimization of the motor design.

**Table 3** presents the range-averaged efficiency values of the baseline motor and the three considered modifications over the fan speed range from  $n_{min} = 600$  rpm to  $n_{max} = 2,300$  rpm.

**Figure 4** shows the stator and rotor slot geometries of the considered motors.

In the third modification, the motor obtained in the second stage is used as the initial configuration, and the optimization procedure is repeated to further refine the stator-winding parameters, the core length  $L$ , the geometrical parameters of the stator slot region (slot height  $H1$  and slot

width  $GP$ ), and the rotor geometry (distance between the circle centers  $A2$ , diameter of the larger circle  $D1$ , and diameter of the smaller circle  $D2$ ).

The values of the design variables obtained from optimization in DIMAS*Drive* using the range-averaged efficiency criterion are presented in **Table 2**.

In some cases, the motor-efficiency criterion must account for the operating time at each specified rotational speed within the control range. This depends on the technological requirements of the driven mechanism. In such cases, a load time diagram, that is, a tachogram, is specified. The range-efficiency criterion of the motor is then calculated by considering the operating duration at each point of the control range according to the following expression:

$$\eta_{tg} = \frac{\sum_i (\eta(n_i) \cdot t_{n_i})}{\sum_i t_{n_i}} \quad (8)$$

where  $t_{n_i}$  is the operating time of the motor at the rotational speed  $n_i$ , and  $i$  is the index of the tachogram segment.

If the drive operates according to the following tachogram—1 h at 600 rpm, 1 h at 1,000 rpm, and 1 h at 2,300 rpm—the values of the range-averaged efficiency criterion are those given in **Table 4**.

The dependence of motor efficiency variation within the control range is shown in **Figure 5**.

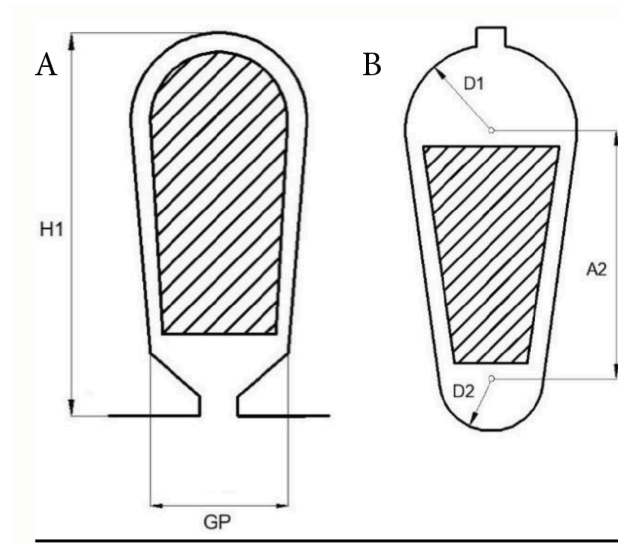
The thermal behavior of the considered modifications is significantly improved, as shown in **Figure 6**

Thus, for the considered drive system, it is preferable to use modified versions of the 4A160M2 motor rather than the baseline 4A180S2 motor, as this choice provides better size, weight, and cost characteristics.

#### 5. Modeling in MATLAB/Simulink

The MATLAB/Simulink environment is employed as a simulation platform to evaluate the energy-performance indicators at the input of the induction motor and the drive system, including efficiency ( $\eta$ ), phase displacement factor ( $\cos\phi$ ), and power coefficient ( $\chi$ ). The fundamental harmonic power components are determined, namely the apparent power  $S_1$  (kVA), active power  $P_1$  (kW), and reactive power  $Q_1$  (kVar). In addition, the total power components for all considered harmonics are evaluated, including the apparent power  $S$  (kVA), active power  $P$  (kW), and non-active power  $D$  (kVar).

The non-active power  $D$  consists of two components,  $Q_1$  and  $T$ , where  $Q_1$  is associated with the

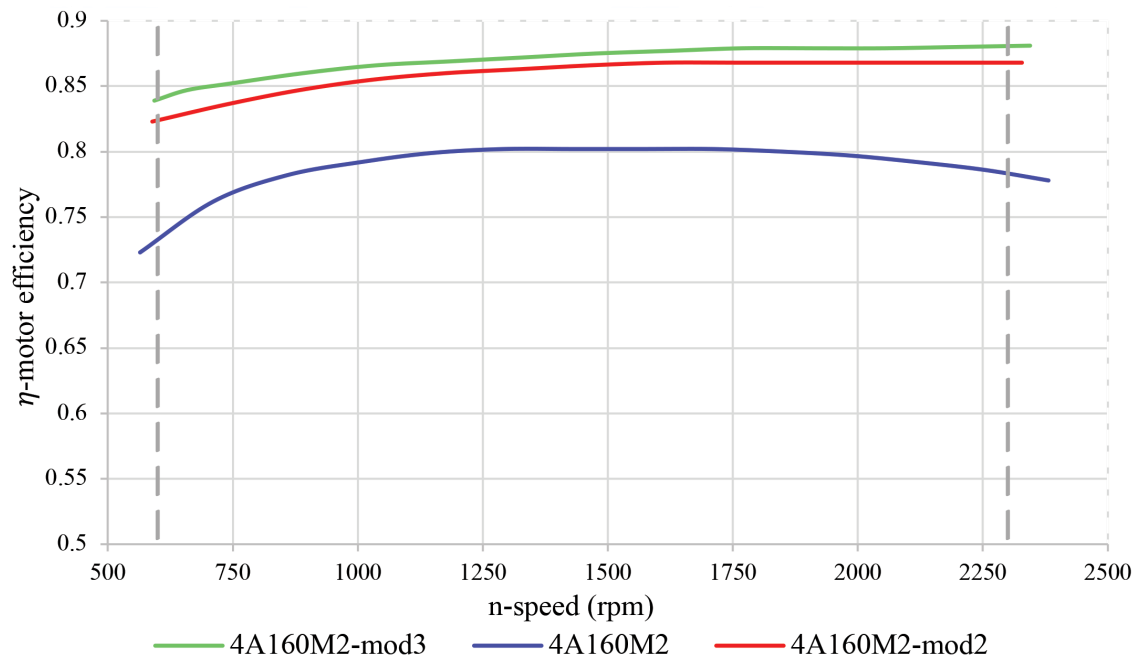


**Figure 4.** Stator (A) and rotor (B) slot geometries for the motors considered

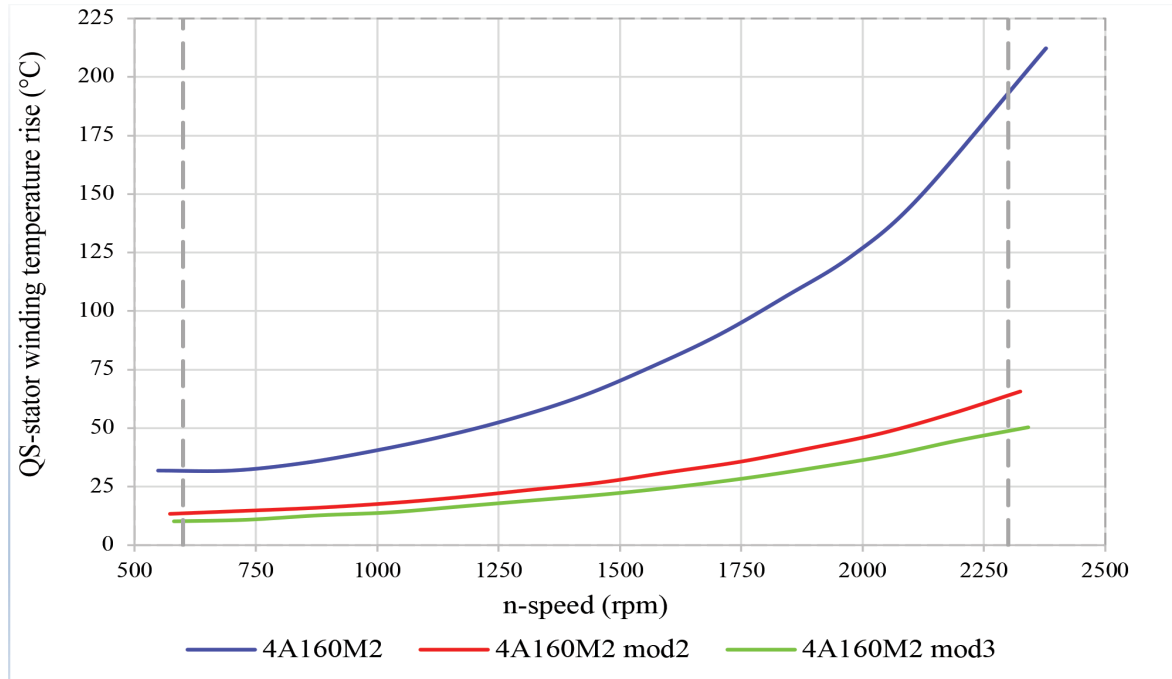
**Table 2.** Design variables of the baseline and modified induction motors

Design variables	$W_{OS}$	$q_{ef}$ mm <sup>2</sup>	$d_{ins}$ mm	L mm	H1 mm	GP mm	ZR	A2 mm	D1 mm	D2 mm
Baseline induction motor 4A160M2	84	2.74	1.4	130	21	11.9	28	22	7	4.9
Modification 2	65	5.64	1.97	154	28.5	13.9	31	19.9	8.3	4.7
Modification 3	57	6.61	2.11	183	29.4	13.9	30	23.5	8.3	4.6

Abbreviations: A2: Distance between the circle centers; D1: Diameter of the larger circle; D2: Diameter of the smaller circle;  $d_{ins}$ : Insulation thickness; GP: Stator slot width; H1: Stator slot height; L: Core length;  $q_{ef}$ : Effective conductor cross-sectional area;  $W_{OS}$ : Number of stator winding turns; ZR: Number of rotor slots.



**Figure 5.** Motor efficiency versus rotor speed in the control range for the baseline motor and its modifications



**Figure 6.** Thermal characteristics of the baseline induction motors and their modified designs

**Table 3.** Range-averaged efficiency values of the induction motors

Baseline induction motor 4A160M2	$\eta_{avg} = 0.793$
Modification 1	$\eta_{avg} = 0.814$
Modification 2	$\eta_{avg} = 0.873$
Modification 3	$\eta_{avg} = 0.883$

**Table 4.** Range-averaged efficiency of the baseline motor and its modifications, considering the tachogram

Baseline induction motor 4A160M2	$\eta_{tg} = 0.771$
Modification 1	$\eta_{tg} = 0.795$
Modification 2	$\eta_{tg} = 0.863$
Modification 3	$\eta_{tg} = 0.875$

phase shift between the fundamental components of current and voltage, and  $T$  represents the distortion power caused by higher harmonics. These components are related by  $D^2 = Q_1^2 + T^2$ . The model of the ASIM drive based on a two-stage frequency converter in the MATLAB/Simulink environment is shown in **Figure 7**. The model includes seven main functional blocks. The first block represents an ideal three-phase power supply with a line voltage of 380 V and a frequency of 50 Hz. The three-phase voltage is converted using a three-phase diode bridge rectifier. A voltage-source inverter, together with a pulse width mod-

ulation (PWM) generator, produces an output voltage at a specified frequency. The capacitance of each capacitor in the DC link is  $C_f = 5.7$  mF. The PWM carrier frequency is 6 kHz. The drive is controlled using a constant-voltage-to-frequency law,  $U/f = \text{const}$ .

The drive is loaded by a two-pole squirrel-cage IM with the following specifications: rated power  $P_n = 18.5$  kW, rated line voltage  $U_n = 380$  V, and rated frequency  $f_n = 50$  Hz.

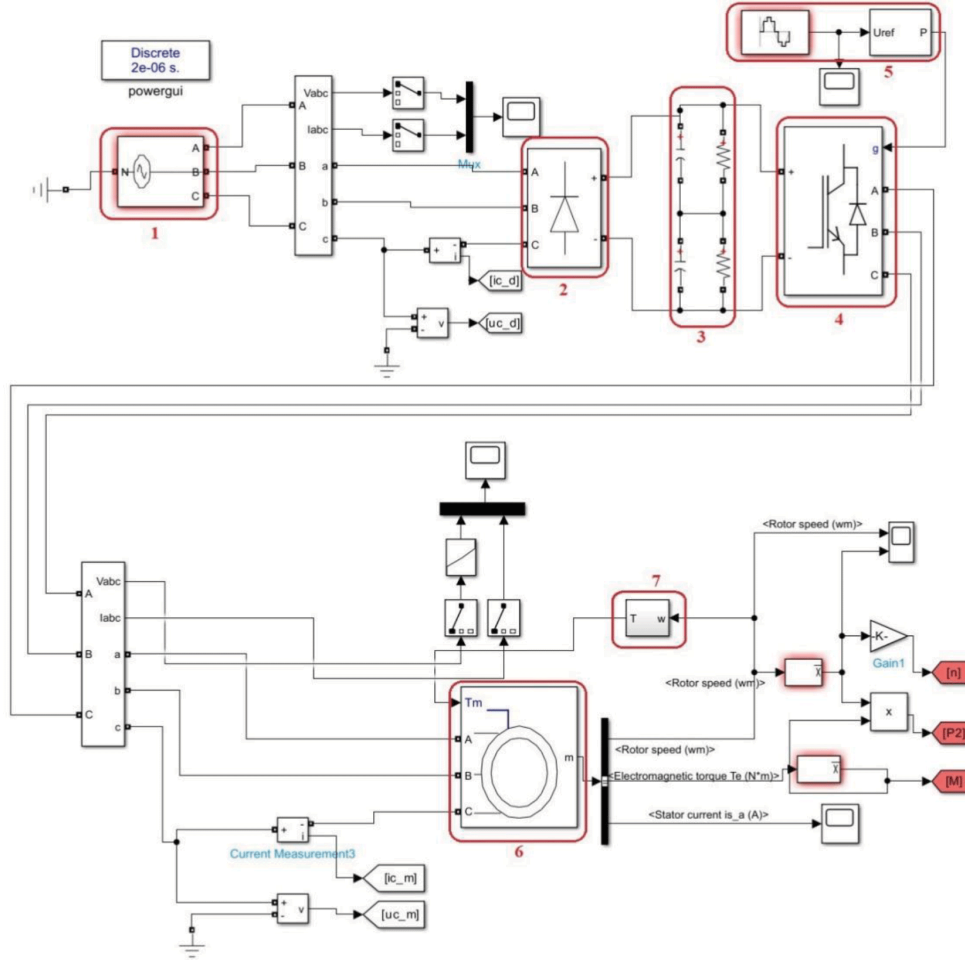
The stator parameters, including the stator resistance and stator leakage inductance, are  $R_s = 0.365 \Omega$ , and  $L_{ls} = 2.13$  mH, respectively. The corresponding rotor parameters are  $R_r = 0.18 \Omega$ , and  $L_{lr} = 2.45$  mH. The mutual inductance is  $L_m = 121.02$  mH. The load torque characteristic is given by  $M(\omega) = 18.1 + 0.757 \cdot 10^{-3} \cdot \omega^2$ .

In the simulation, the load type is selected according to the specific application of the drive and may vary in magnitude and type. The system of differential equations is solved using the “discrete (no continuous states)” method with a variable time step. A time step of 2  $\mu$ s is used for the calculations. The motor speed is controlled within the range of 600–2,300 rpm by adjusting the converter output frequency from 10 to 40 Hz.

In the MATLAB/Simulink simulations, measurement blocks were used to acquire instantaneous voltage and current signals from sensors, as described.<sup>20–23</sup>

The calculated power values enable evaluation of key performance indicators at the motor and drive system inputs, including efficiency, dis-





**Figure 7.** Simulation model of the adjustable-speed induction motor drive with a two-stage frequency converter. 1: Three-phase voltage source; 2: Rectifier; 3: Direct current-link filter; 4: Voltage-source inverter; 5: Pulse width modulation generator; 6: Induction motors; 7: Load

placement power factor, total harmonic distortion (THD), and power components. Based on waveform analysis, the THD factors are determined as follows:

$$THD_U = \sqrt{\sum \left( \frac{U_\nu}{U_1} \right)^2}, THD_I = \sqrt{\sum \left( \frac{I_\nu}{I_1} \right)^2} \quad (9)$$

The power factors are calculated from the harmonic spectra of voltages and currents using the methods described<sup>24–26</sup>:

$$\chi = \frac{\cos \varphi}{\sqrt{1 + THD_U^2 + THD_I^2 + THD_U^2 \cdot THD_I^2}} \quad (10)$$

For a system supplied by an infinite bus, supplying a distorted load with an undistorted three-phase voltage, the power factor of the electric drive is calculated accordingly<sup>27–29</sup>:

$$\chi = \frac{\cos \varphi}{\sqrt{1 + THD_I^2}} \quad (11)$$

The DIMASDrive software is used to determine the parameters of the equivalent circuit.

The equivalent circuit parameters of the baseline induction motor and its modified designs, used as input data for simulations. In the MATLAB/Simulink environment, the results are presented in **Table 5**.

The simulation results of the drives employing the baseline motor 4A160M2 and its two modifications in the MATLAB/Simulink environment are presented in **Tables 6, 7, 8**. These tables present the energy performance indicators at the drive input for the considered drive configurations, as well as the frequency converter efficiency.

**Tables 6, 7, 8** show differences in current, power, and rotational speed (rpm). However, the energy performance indicators remain nearly identical across the simulation results for the drives with the baseline induction motor and its two modified designs.

In MATLAB/Simulink, the power factor at the drive input can be determined either from the power balance or from the  $THD_I$  and  $\cos \varphi$  values.



**Table 5.** Equivalent circuit parameters of the baseline and modified induction motor

Parameters	motor	$R_s(\Omega)$	$R_r(\Omega)$	$L_{1s}(\text{mH})$	$L_{1r}(\text{mH})$	$L_m(\text{mH})$
Baseline induction motor 4A160M2		0.365	0.18	2.13	2.45	121.02
Modification 2		0.12	0.117	1.4	1.66	28.34
Modification 3		0.096	0.093	1.18	1.59	27.29

Abbreviations:  $R_r$  : Rotor resistance;  $R_s$  : Stator resistance;  $L_m$  : Mutual inductance;  $L_{1r}$  : Rotor leakage inductance;  $L_{1s}$ : Stator leakage inductance.

**Table 6.** Drive input parameters for the baseline induction motor 4A160M2

f, Hz	U, V	I, A	P, kW	n, rpm	$\cos\varphi$	THDi	$\chi$	$\eta_{FC}$
10	218.3	4.4	1.6	551	0.998	1.542	0.543	0.978
15	218.3	7.0	2.6	849	0.996	1.476	0.559	0.986
20	218.3	10.9	4.1	1,140	0.995	1.403	0.577	0.977
25	218.3	15.6	6.1	1,427	0.993	1.335	0.595	0.996
30	218.3	22.0	8.9	1,709	0.989	1.26	0.615	0.996
35	218.3	31.7	13.3	2,041	0.986	1.167	0.642	0.997
40	218.3	39.4	17.0	2,256	0.983	1.105	0.659	0.996
45	218.3	51.2	22.9	2,516	0.981	1.026	0.684	0.991

Abbreviations:  $\chi$ : Power factor;  $\cos\varphi$ : Phase displacement factor; f: Converter output frequency; I: Drive input current; n: Motor rotational speed;  $\eta_{FC}$ : Frequency converter efficiency; P: Total active power at the drive input; THDi: Total harmonic distortion of current; U: Drive input voltage.

**Table 7.** Drive input parameters for the modified induction motor (modification 2)

f, Hz	U, V	I, A	P, kW	n, rpm	$\cos\varphi$	THDi	$\chi$	$\eta_{FC}$
10	218.3	4.4	1.5	573	0.997	1.544	0.542	0.968
15	218.3	7.0	2.6	870	0.996	1.476	0.559	0.969
20	218.3	10.7	4.0	1,164	0.995	1.406	0.577	0.971
25	218.3	15.4	5.9	1,456	0.993	1.338	0.594	0.989
30	218.3	21.5	8.6	1,746	0.99	1.264	0.614	0.998
35	218.3	28.9	12.0	2,030	0.987	1.191	0.635	0.997
40	218.3	40.2	17.4	2,373	0.984	1.099	0.662	0.986

Abbreviations:  $\chi$ : Power factor;  $\cos\varphi$ : Phase displacement factor; f: Converter output frequency; I: Drive input current; n: Motor rotational speed;  $\eta_{FC}$ : Frequency converter efficiency; P: Total active power at the drive input; THDi: Total harmonic distortion of current; U: Drive input voltage.

## 6. Calculation of the range-based discounted cost criterion

The choice of design criteria is crucial in the design of ASIMs. In addition to the traditional motor-efficiency criterion, an innovative DCC can be used for the drive. Building upon the criterion introduced,<sup>10</sup> the present work extends the discounted cost formulation to incorporate, alongside capital and energy efficiency components, the monetary costs of both reactive-power and distortion-power compensation—factors that jointly govern the electromagnetic compatibility of the drive with the supply network.<sup>10,11,30</sup> Be-

cause of the operating characteristics of ventilation systems, these criteria are range-based and depend on the drive's operating mode.<sup>13</sup>

If the active power consumed by the drive,  $P_1$ , is known, the reactive power  $Q_1$  and the distortion power  $T$  can be determined accordingly<sup>24,31</sup>:

$$Q_1 = P_1 \cdot tg\varphi, \quad T = P_1 \cdot \sqrt{tg^2\chi - tg^2\varphi} \quad (12)$$

Based on the control characteristic  $P_1=f(n)$  and the specified drive tachogram, the active power consumed by the drive is calculated either as a range-averaged value or as a range-based

**Table 8.** Drive input parameters for the modified induction (modification 3)

f, Hz	U, V	I, A	P, kW	n, rpm	cosφ	THDi	χ	η <sub>FC</sub>
10	218.3	4.3	1.5	579	0.997	1.547	0.542	0.968
15	218.3	6.9	2.5	877	0.996	1.477	0.558	0.968
20	218.3	10.6	4.0	1,172	0.995	1.407	0.577	0.971
25	218.3	15.3	5.9	1,465	0.993	1.339	0.594	0.988
30	218.3	21.5	8.6	1,758	0.99	1.264	0.614	0.999
35	218.3	28.9	12.0	2,045	0.987	1.19	0.635	0.997
40	218.3	40.3	17.5	2,393	0.984	1.098	0.662	0.986

Abbreviations: χ: Power factor; cosφ: Phase displacement factor; f: Converter output frequency; I: Drive input current; n: Motor rotational speed; η<sub>FC</sub>: Frequency converter efficiency; P: Total active power at the drive input; THDi: Total harmonic distortion of current; U: Drive input voltage.

value weighted by the tachogram:

$$P_{1avg} = \frac{1}{n_2 - n_1} \cdot \int_{n_1}^{n_2} P_1(n_i) dn \quad (13)$$

$$P_{1tg} = \frac{\sum_i (P_1(n_i) \cdot t_{n_i})}{\sum_i t_{n_i}}. \quad (14)$$

Using the corresponding control characteristics, the required energy-performance indicators can be determined either as range-averaged values:

$$\eta_{avg} = \frac{1}{n_2 - n_1} \cdot \int_{n_1}^{n_2} \eta(n_i) dn \quad (15)$$

$$\chi_{avg} = \frac{1}{n_2 - n_1} \cdot \int_{n_1}^{n_2} \chi(n_i) dn \quad (16)$$

$$\cos\varphi_{avg} = \frac{1}{n_2 - n_1} \cdot \int_{n_1}^{n_2} \cos\varphi(n_i) dn \quad (17)$$

or as range-based values weighted by the tachogram:

$$\eta_{tg} = \frac{\sum_i (\eta(n_i) \cdot t_{n_i})}{\sum_i t_{n_i}} \quad (18)$$

$$\chi_{tg} = \frac{\sum_i (\chi(n_i) \cdot t_{n_i})}{\sum_i t_{n_i}} \quad (19)$$

$$\cos\varphi_{tg} = \frac{\sum_i (\cos\varphi(n_i) \cdot t_{n_i})}{\sum_i t_{n_i}} \quad (20)$$

The drive DCC, which can likewise be evaluated either as a range-averaged quantity or as a range-based quantity weighted by the tachogram, is calculated using the following expressions:

$$DCC_{avg} = \frac{1}{n_2 - n_1} \cdot \int_{n_1}^{n_2} DCC(n_i) dn \quad (21)$$

$$DCC_{tg} = \frac{\sum_i (DCC(n_i) \cdot t_{n_i})}{\sum_i t_{n_i}} \quad (22)$$

If the total cost of the drive, *CED*, is known, the DCC at a given operating point of the control range can be written as follows:

$$DCC = (CED + C_{rpc1} + C_{rpc2}) \cdot [1 + (k_d + k_s)] + C_L \quad (23)$$

where *C<sub>rpc1</sub>* is the cost associated with reactive-power compensation, c.u.; *C<sub>rpc2</sub>* is a novel component representing the cost of distortion-power compensation, c.u., introduced in this study; *C<sub>L</sub>* is the cost of annual energy losses, c.u.; *k<sub>d</sub>* is the share of depreciation costs; and *k<sub>s</sub>* is the share of maintenance and operating costs. For the ASIM drive, *k<sub>d</sub>* = 0.065 and *k<sub>s</sub>* = 0.069 are assumed, the same values used for general-purpose IMs.

If the load-time diagram of drive operation is known, that is, if the drive tachogram is specified, the expressions for *C<sub>rpc1</sub>* and *C<sub>rpc2</sub>* take the following form:

$$C_{rpc1} = c_{k1} \cdot k_{my} \cdot P_{1tg} [tg(\arccos\varphi_{tg} - tg\varphi_0)] \cdot t_{ED} \quad (24)$$

where *c<sub>k1</sub>* is the unit cost of installing 1 kVar of reactive-power compensation equipment (10 c.u. is used in the calculations); *k<sub>my</sub>* is the participation factor of the ASIM drive in the maximum load demand (0.25 is used in the calculations); and *φ<sub>0</sub>* is the phase angle between current and voltage at which reactive-power compensation is not required (*tg φ<sub>0</sub>* = 0.484 is assumed in the calculations).

The newly proposed component *C<sub>rpc2</sub>* makes it possible to account for the cost of distortion-power compensation in accordance with the electromagnetic-compatibility requirements determined by THD:

**Table 9.** Performance indicators of the drive with the baseline 4A160M2

Drive	Range Is set	Tachogram Is set	Range Is set taking into account inflation	Tachogram Is set taking into account inflation
<b>Parameters</b>				
$\eta$	0.784	0.762	0.784	0.762
$CED, \text{c.u.}$	4,800	4,800	4,800	4,800
$\cos\varphi$	0.99	0.992	0.99	0.992
$P_1, \text{kW}$	9.57	7.375	9.57	7.375
$\chi$	0.609	0.591	0.609	0.591
$C_{rpc2}, \text{c.u.}$	57,143	46,425	57,143	46,425
$C_L, \text{c.u.}$	4,898	4,100	4898	4,100
$K, \text{c.u.}$	61,943	51,225	61,943	51,225
$Y, \text{c.u.}$	13,198	10,964	14,016	11,644
$DCC, \text{c.u.}$	75,142	62,189	75,960	62,869

Abbreviations:  $CED$ : Drive cost;  $C_L$ : Cost of active-power losses;  $\cos\varphi$ : Phase displacement factor;  $C_{rpc2}$ : Cost of distortion-power compensation;  $DCC$ : Discounted costs criterion;  $K$ : Capital investment;  $P_1$ : Active power consumed by the drive;  $Y$ : Annual operating cost;  $\eta$ : Drive efficiency;  $\chi$ : Power factor.

$$C_{rpc2} = c_{k2} \cdot k_{my} \cdot P_{1tg} \cdot \left\{ \sqrt{[tg(\arccos\chi_{tg})]^2 - [tg(\arccos\varphi_{tg})]^2} - tg[\arccos\left(\frac{1}{\sqrt{1+THD_{ID}^2+THD_{UD}^2+THD_{ID}^2 \cdot THD_{UD}^2}}\right)] \right\} \cdot t_{ED} \quad (25)$$

where  $c_{k2}$  is the unit cost of installing 1 kVar of distortion-power compensation equipment (10 c.u. is used in the calculations).

In mechatronic systems supplied from an infinite-bus system, the supply voltage can be considered sinusoidal. Under these conditions, the THD of the voltage,  $THD_{UD}$  may be taken as zero and can therefore be omitted from the above expression. Standards<sup>32,33</sup> specify the permissible values of the THD of current,  $THD_{ID}$ .

If the load-time diagram of drive operation is known, the annual cost of active-power losses is determined as follows:

$$C_L = c_{ae} \cdot P_{1tg} \cdot (1 + a_r - \eta_{tg}) \cdot t_{ED} \quad (26)$$

where  $c_{ae}$  is the cost of 1 kWh of active electrical energy (1 c.u. is used in the calculations);  $a_r$  is the coefficient accounting for losses in distribution networks (0.04 is used in the calculations); and  $t_{ED}$  is the annual operating time of the drive (2,000 h is used in the calculations).

If the motor operating time diagram is not specified in advance, the range-averaged values of the discounted cost components  $C_{rpc1}$ ,  $C_{rpc2}$  and  $C_L$  are calculated using  $\eta_{avg}$ ,  $\chi_{avg}$ ,  $\cos\varphi_{avg}$ , and  $P_{1avg}$ .

Given that the economic payback horizon for adjustable-speed drives typically spans 5–8 years, the DCC should incorporate inflationary effects to ensure realistic long-term cost projections.<sup>34,35</sup>

Therefore, the DCC of the ASIM drive can generally be written as follows:

$$DCC = K + \sum_{i=1 \dots T_n} Y_i \quad (27)$$

where  $K = cep + C_{rpc1} + C_{rpc2}$  is the initial capital investment and  $Y_i = (k_d + k_s) \cdot (cep + C_{rpc1} + C_{rpc2}) + C_L$  is the annual operating cost.

If inflation is neglected, the annual cost remains constant,  $Y_i = const$ , and equals the first-year value  $Y_1$  determined for the initial year of operation. To account for annual inflation, the DCC can be written as follows:

$$DCC = K + Y_1 \cdot \frac{1 + (1 + d_{INF1}) + \dots + (1 + d_{INF(T_n-1)})}{T_n} \quad (28)$$

where  $d_{INF1}, \dots, d_{INF(T_n-1)}$  are the forecast inflation rates for the respective years within the payback period  $T_n$ .

For simplicity, an average annual inflation rate  $d_{INF1}$ , over the payback period, may be assumed. In this case, the inflation coefficient is determined as follows:

$$k_{INF} = \frac{\sum_{m=0}^{T_n-1} \left(1 + \frac{d_{INF}}{100\%}\right)^m}{T_n} \quad (29)$$

where  $d_{INF}$  is the average annual inflation rate, %.

Two operating modes are considered. In the first case, the drive operates over the rotor-speed

**Table 10.** Performance indicators of the adjustable-speed induction motor drive with modification 2 of the baseline 4A160M2

Drive	Range Is set	Tachogram Is set	Range Is set taking into account inflation	Tachogram Is set taking into account inflation
<b>Parameters</b>				
$\eta$	0.858	0.841	0.858	0.841
$CED, \text{c.u.}$	4,900	4,900	4,900	4,900
$\cos\varphi$	0.992	0.993	0.992	0.993
$P_1, \text{kW}$	7.466	7.017	7.466	7.017
$\chi$	0.598	0.589	0.598	0.589
$C_{rpc2}, \text{c.u.}$	46,074	44,448	46,074	44,448
$C_L, \text{c.u.}$	2,718	2,793	2,718	2,793
$K, \text{c.u.}$	50,974	49,348	50,974	49,348
$Y, \text{c.u.}$	9,548	9,405	10,140	9,988
$DCC, \text{c.u.}$	60,522	58,754	61,114	59,337

Abbreviations:  $CED$ : Drive cost;  $C_L$ : Cost of active-power losses;  $\cos\varphi$ : Phase displacement factor;  $C_{rpc2}$ : Cost of distortion-power compensation;  $DCC$ : Discounted costs criterion;  $K$ : Capital investment;  $P_1$ : Active power consumed by the drive;  $Y$ : Annual operating cost;  $\eta$ : Drive efficiency;  $\chi$ : Power factor.

**Table 11.** Performance indicators of the adjustable-speed induction motor drive with modification 3 of the baseline 4A160M2

Drive	Range Is set	Tachogram Is set	Range Is set taking into account inflation	Tachogram Is set taking into account inflation
<b>Parameters</b>				
$\eta$	0.868	0.853	0.868	0.853
$CED, \text{c.u.}$	5,000	5,000	5,000	5,000
$\cos\varphi$	0.992	0.993	0.992	0.993
$P_1, \text{kW}$	7.455	6.894	7.455	6.894
$\chi$	0.597	0.587	0.597	0.587
$C_{rpc2}, \text{c.u.}$	46,137	43,916	46,137	43,916
$C_L, \text{c.u.}$	2,564	2,578	2,564	2,578
$K, \text{c.u.}$	51,137	48,917	51,137	48,917
$Y, \text{c.u.}$	9,417	9,133	10,001	9,699
$DCC, \text{c.u.}$	60,554	58,050	61,137	58,616

Abbreviations:  $CED$ : Drive cost;  $C_L$ : Cost of active-power losses;  $\cos\varphi$ : Phase displacement factor;  $C_{rpc2}$ : Cost of distortion-power compensation;  $DCC$ : Discounted costs criterion;  $K$ : Capital investment;  $P_1$ : Active power consumed by the drive;  $Y$ : Annual operating cost;  $\eta$ : Drive efficiency;  $\chi$ : Power factor.

range 600–2,300 rpm, and the average values of the energy-performance indicators and the active power consumed by the ASIM drive are determined for this interval. In the second case, the drive operates according to a specified tachogram (3,600 s–600 rpm, 3,600 s–1,000 rpm, 3,600 s–2,300 rpm), and the energy performance indicators and the consumed active power are calculated using the corresponding expressions. In this case, reactive power compensation can be neglected because  $\text{tg}\varphi_0$  is significantly less than 0.484. If the average inflation rate is assumed to be 3% and the payback period is  $T_n = 5$  years, the inflation coefficient is  $k_{INF} = 1.062$ . In the subsequent calculations, the

permissible THD is set to  $THD_{ID} = 10\%$ . The cost of the drive with the baseline IM 4A160M2 is assumed to be 4,800 c.u., including 4,000 c.u. for the frequency converter and 800 c.u. for the baseline motor. The calculation results are presented in **Tables 9,10,11**.

One reason for the difference between the efficiency values calculated in MATLAB/Simulink and those obtained in DIMAS*Drive* is that the MATLAB/Simulink model does not account for core losses, mechanical losses, or additional stray losses in the IM. Therefore, to properly evaluate the discounted cost criterion, it is proposed to recalculate the drive efficiency as the product

of the converter efficiency obtained from MATLAB/Simulink and the IM efficiency obtained from DIMAS*Drive*.

Similarly, the performance indicators were calculated for the ASIM drive with the second modification of the baseline motor (**Table 10**). In this case, the inflation coefficient and the permissible current THD remain the same as in the previous calculation. The cost of the drive is assumed to be 4,900 c.u., because the cost of the second modification of the baseline motor is 100 c.u. higher.

Similarly, the performance indicators were calculated for the ASIM drive with the third modification of the baseline motor (**Table 11**). In this case, the inflation coefficient and the permissible current THD also remain unchanged. The cost of the drive is assumed to be 5,000 c.u. because the third modification to the baseline motor costs 200 c.u. higher.

## 7. Conclusion

The overall performance of adjustable-speed ventilation drives can be comprehensively evaluated using the proposed DCC. This criterion accounts for capital cost, the cost of active power losses determined by energy efficiency, and the costs associated with reactive power and distortion power compensation. These components reflect both the drive's energy performance and its electromagnetic compatibility with the supply network. Currently, no widely accepted method exists for quantifying the electromagnetic compatibility component in monetary terms. As a result, this component may be underestimated in conventional evaluations. The present study proposes an approach for its calculation and inclusion in the discounted cost criterion.

The performance of the drive is improved through the use of ASIMs developed as modifications of baseline IMs by means of structural and parametric optimization implemented in DIMAS*Drive* using the efficiency criterion. In addition, the DCC is evaluated for each design variant through simulation in MATLAB/Simulink. The design variants are assessed against this criterion, and the optimal solution is selected as the one with the minimum discounted cost.

For modeling and subsequent optimization of the ASIM drive, the ventilation unit should be represented by the load characteristic  $n = f(M)$ . Structural and parametric optimization carried out in DIMAS*Drive* increases the range-averaged efficiency of the IM. The range-averaged efficiency of the baseline motor is 79.3%, increasing to 87.3% for the second modification and 88.3% for

the third. Similar trends are observed when the drive operates in accordance with the specified tachogram.

For all ASIM drive variants considered, the input power factor, displacement factor, and THDi are nearly identical. Because the displacement factor is close to unity, the cost of reactive power compensation can be neglected. Within the proposed DCC, the cost of distortion-power compensation must be explicitly included, as it determines the drive's electromagnetic compatibility with the supply network.

For the range-averaged operating mode, the proposed DCC decreases by 19.46% when the second modification is used instead of the baseline motor, and by 19.41% when the third modification is used, the latter reduction being smaller due to the higher motor cost of the third modification. Therefore, the second modification is the preferred option for this operating mode. For the operating mode defined by the tachogram, the results are different: the range-based DCC decreases by 5.52% for the second modification and by 6.66% for the third modification relative to the baseline motor. Therefore, the third modification is preferable for this operating mode.

For the adopted permissible  $THD_i$  value of 10% and the assumed installation cost of 10 c.u. per 1 kVar of distortion-power compensation equipment, this component accounts for more than 70% of the total discounted cost criterion. When inflation is taken into account, the discounted costs increase. However, the ratio between the discounted costs of ASIM drives with optimized motors and that of the drive with the baseline motor 4A160M2 remains almost unchanged.

In general, the considered drive variants can be effectively evaluated using the proposed range-based discounted cost criterion. This criterion can therefore be applied both to the analysis of existing drives and to the design of new ASIM drives.

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The authors declare they have no competing interests

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## Availability of data

The data supporting the findings of this study are available from the corresponding author upon reasonable request.

## AI tools statement

All authors confirm that no AI tools were used in the preparation of this manuscript.

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